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Control of Spin-1/2 Quantum System Using Lyapunov Method to Achieve Quantum NOT Gate Operation
ANDREAS P SANDIWAN, Dr.Eng. Ir. Adha Imam Cahyadi, S.T., M.Eng., IPM. ; Dr.Eng. Ir. F. Danang Wijaya, S.T., M
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